

# Doping effects on dynamical physical properties of $\text{Ca}_{0.6}\text{Sr}_{0.4}\text{Bi}_4\text{Ti}_4\text{O}_{15}$ ferroelectric ceramics with layered-perovskite structure

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**Abstract** The change of electrical and lattice dynamical properties of ferroelectric  $\text{Ca}_{0.6}\text{Sr}_{0.4}\text{Bi}_4\text{Ti}_4\text{O}_{15}$  (CSBT) ceramics were studied by doping with 0.1 wt.% of  $\text{CeO}_2$  and  $\text{MnO}_2$ . The loss tangent and the AC conductivity decreased markedly due to the reduction of charge carrier. The activation energy of doped-CSBT increased owing to the reduction of intrinsic defects in the crystal lattice. For doped and pure CSBT, the appearance of thermal hysteresis and the satisfaction of the Curie-Weiss law by the dielectric susceptibility data assigned the first order nature of a ferroelectric phase transition. Especially in ferroelectric phases, the soft optic phonon mode showed the significant softening towards  $T_1$  (at  $T_1$ , the square of soft mode frequency  $\omega_s^2 \rightarrow 0$ ) and  $\omega_s^2$  was approximately proportional to  $T_1 - T$ , where  $T_1$  is  $\sim 70^\circ\text{C}$  above  $T_C = 672^\circ\text{C}$ , demonstrated a first order displacive nature of a ferroelectric phase transition. The invariance of lattice dynamical feature indicated that the crystal lattice did not influence markedly by the doping ions.

**Keywords** Layered-ferroelectrics · AC in conductivity · Phase transition · Soft mode

## 1 Introduction

Aurivillius bismuth layered-structure compounds (BLSFs) have attracted much attention for its high Curie temperature

$T_C$ , fatigue-free, and environmentally friendly nature, and become potential candidates for the application of electric and piezoelectric devices [1–4]. The chemical formula of this series is expressed as  $\text{Bi}_2\text{A}_{m-1}\text{B}_m\text{O}_{3m+3} = (\text{Bi}_2\text{O}_2)^{2+}(\text{A}_{m-1}\text{B}_m\text{O}_{3m+1})^{2-}$ ; A is mono-, di- and trivalent ions or a mixture of them, B is tetra-, penta-, and hexavalent ions, the subscript  $m$  and  $m-1$  are the numbers of oxygen octahedra and pseudo-perovskite units in the pseudo-perovskite layers, respectively. The crystal structure of BLSFs consists of pseudo-perovskite layers interleaved with the bismuth oxide  $(\text{Bi}_2\text{O}_2)^{2+}$  layers along the  $c$ -axis [5–9]. The  $\text{CaBi}_4\text{Ti}_4\text{O}_{15}$  (CBT) is one of the important member of BLSFs family for high temperature piezoelectric applications owing to its low electric conductivity, low dielectric loss, high  $T_C$  ( $790^\circ\text{C}$ ), and easy to fabrication by the conventional solid state reaction [10–13]. However, the relatively low piezoelectric response and large temperature dependence is the main obstacle for the commercialization [14]. The piezoelectric properties of CBT are largely enhanced by the partial replacement of the A-site calcium ( $\text{Ca}^{2+}$ ) ion with the strontium ( $\text{Sr}^{2+}$ ) ion, nevertheless  $T_C$  reduces owing to the large ionic radius ( $\text{Ca} = 1.04$  and  $\text{Sr} = 1.20 \text{ \AA}$ ). The Sr-doped CBT with the composition  $\text{Ca}_{0.6}\text{Sr}_{0.4}\text{Bi}_4\text{Ti}_4\text{O}_{15}$  (CSBT) shows the best piezoelectric performance, and the observed piezoelectric coefficient and the dc resistivity is decuply higher than the CBT and  $\text{SrBi}_4\text{Ti}_4\text{O}_{15}$  (SBT) [11]. Therefore, CSBT is appeared as a potential candidate for high temperature applications. However, further modification is necessary for better ferroelectric and electrical performance.

Element doping is known to an effective route to improve piezoelectric and ferroelectric properties. In general, doping could be in oxide layers and/or in perovskite layers (A- or B-sites). Subbaro reported that the  $T_C$  of BLSFs decreases when the size of the A-site cations increase [15], while Forbess et al. found that the  $T_C$  increases and the electrical properties are improved markedly due to the replacement of

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A-site cation by a small size ion [16]. In this contrast,  $\text{MnO}_2$  can be a typical additive due to the multi-valence nature of Mn ions; such as  $\text{Mn}^{2+}$ ,  $\text{Mn}^{3+}$ , and  $\text{Mn}^{4+}$ , which may be very effective to regulate electrical properties. On the other hand, the ionic radius of  $\text{Ce}^{4+}$  ion is close to that of  $\text{Ca}^{2+}$  ion but effective charge is different, which could be effective to regulate the oxygen vacancy and improve electrical performance [17]. By considering these phenomena,  $\text{MnO}_2$  and  $\text{CeO}_2$  have been chosen as the doping element to improve the ferroelectric and the dielectric properties. Although, a ferroelectric to paraelectric phase transition of CSBT is reported at  $667^\circ\text{C}$  [14], the phase transition dynamics is yet to be clarified.

In this study, we have investigated the  $\text{CeO}_2$  and  $\text{MnO}_2$  doping effect on the phase transition and the dielectric properties of CSBT using an X-ray diffraction (XRD), a scanning electron microscopy (SEM), dielectric, and Raman scattering measurements.

## 2 Experimental

$\text{CeO}_2$  and  $\text{MnO}_2$  (0.1 wt.%) doped CSBT ceramics (abbreviated as CSBT-Ce and CSBT-Mn, respectively) were prepared by a conventional solid state reaction method at Shanghai Institute of Ceramics, Chinese Academy of Sciences [18]. The high purity raw materials,  $\text{Bi}_2\text{O}_3$ ,  $\text{CaCO}_3$ ,  $\text{SrCO}_3$ ,  $\text{TiO}_2$ ,  $\text{CeO}_2$  and  $\text{MnO}_2$  powdered were mixed according to a stoichiometric ratio with the nominal compositions, followed by ball milling for 24 h, and then dried and calcined at  $800\text{--}900^\circ\text{C}$  for 2 h. The calcined mixture was crushed by ball milling for 24 h, and then mixed with 5 wt. % polyvinyl alcohol (PVA) binder for pressing into disks of 12 mm in diameter and 2 mm thickness. The disk samples were finally sintered at  $1100$  to  $1220^\circ\text{C}$  for 30 min in air. The relative density of the sintered samples was about 96–97% of the theoretical value.

The phase purity and the crystal structure were examined by X-ray diffractometer (Panalytical, Philips) with Cu K alpha radiation. The micro-structural investigation was conducted by SEM (JSM-5610, JEOL). For SEM study all the samples were coated with gold film (15 nm) by sputtering. Then the coated samples were placed in the vacuum chamber and SEM measurements were performed with 20 kV operating voltage and 21 mm distance. The dielectric properties were measured by using an impedance/gain phase analyzer (SI1260, Solartron) with heating and cooling rate  $1^\circ\text{C}/\text{min}$  up to  $860^\circ\text{C}$  using a compact furnace with PID controller. The light source used for Raman scattering was a diode-pumped solid-state laser (Torus, Laser Quantum) with a wavelength of 532 nm and a power of approximately 50 mW. The right angle scattering was measured with a triple-grating spectrometer (T64000, Jovin-Yvon). The

spectral resolution was  $2\text{ cm}^{-1}$  for all measurements. The Raman signals were detected using a photomultiplier (R464S, Hamamatsu Photonics). For the temperature dependence of Raman scattering, a heating and cooling stage (THMS600, Linkam) was used to change the temperature of a sample in the range from 20 to  $600^\circ\text{C}$ . The temperature stability is within  $\pm 1^\circ\text{C}$ .

## 3 Results and discussion

### 3.1 XRD and SEM

The XRD patterns of the three samples are shown in Fig. 1, where the diffraction peaks are indexed referring to JCPDS Card no. 43-0973 ( $\text{SrBi}_4\text{Ti}_4\text{O}_{15}$ ). All samples are in a single phase and no secondary phase is detectable. The micrographs of SEM are shown in Fig. 2, a uniform, identical, and plate like grain morphologies are observed for all samples. The impurity free and a single phase diffraction pattern with the identical grain morphology demonstrate that both the Ce and the Mn ions are homogeneously dissolved in the pseudo-perovskite crystal lattice. The site occupancy is discussed in the following section by considering the ionic radius and the analysis of dielectric and Raman data.

### 3.2 Dielectric properties

Figure 3 shows the temperature dependences of dielectric constants of CSBT, CSBT-Ce, and CSBT-Mn measured at 500 kHz, and sharp dielectric anomalies are observed around  $672$ ,  $668$  and  $687^\circ\text{C}$ , respectively, corresponding to an orthorhombic to tetragonal phase transition. The observed  $T_C$  of CSBT is in good agreement with the results reported in literature [11, 12, 14]. It is found that  $T_C$  remains constant with the  $\text{MnO}_2$  doping, while it goes to a  $15^\circ\text{C}$

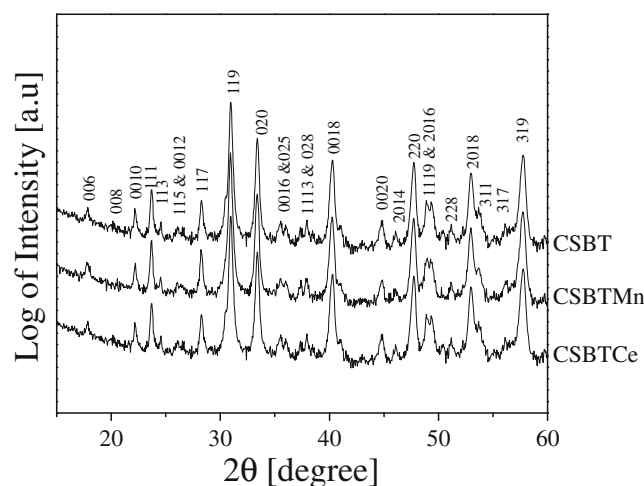
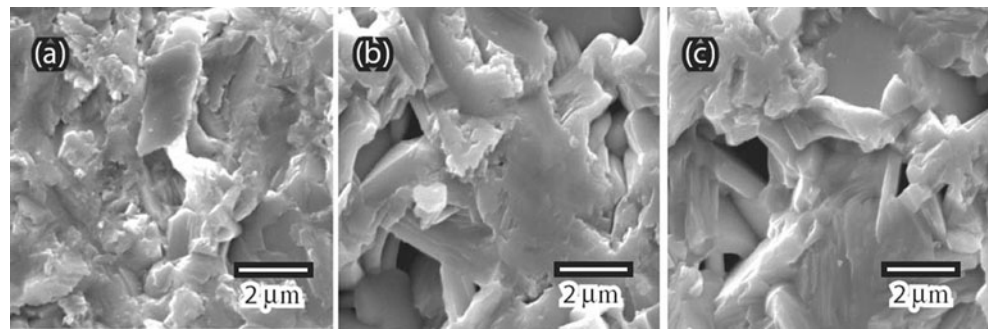


Fig. 1 XRD patterns of CSBT, CSBT-Mn and CSBT-Ce ceramics

**Fig. 2** SEM micrographs of (a) CSBT, (b) CSBT-Mn, and (c) CSBT-Ce ceramics



higher due to the CeO<sub>2</sub> doping. It has been reported that Mn-ion exists as Mn<sup>3+</sup> ion and occupies both of the A and B-sites in a perovskite unit. As a result, there is no noticeable structural change and the *T<sub>C</sub>* does not alter significantly [18]. In contrast, the variation of *T<sub>C</sub>* due to the CeO<sub>2</sub>-doping can be explained by considering the ionic radius of the constituent atoms. The ionic radius of Ce<sup>4+</sup> (0.97 Å) ion is close to the A-site Ca<sup>2+</sup> (1.12 Å) and Bi<sup>3+</sup> (1.17 Å) ions [19]. Therefore, Ce<sup>4+</sup> may replace A-site ions Bi<sup>3+</sup> and/or Ca<sup>2+</sup> ion. It is due to the small ionic radius of Ce<sup>4+</sup> ion that augmented the distortion of TiO<sub>6</sub>, and *T<sub>C</sub>* accelerates from 672 to 687°C [20].

The dielectric maximum ( $\epsilon_m$ ) of CSBT-Ce and CSBT-Mn varied markedly due to the doping and it goes to the minimum for CSBT-Mn. These decreases of dielectric maxima can be explained in account of the polarizability. The dielectric response depends on the four kinds of polarization: electronic, ionic, dipolar and space charge polarization [17]. The effectiveness of each components have a characteristic frequency range i.e. electronic, ionic, dipolar and space charge polarization follows the optical, infrared, microwave and kilohertz or even lower frequency ranges, respectively [21]. As the measured frequency is 500 kHz, therefore, the observed lowering of dielectric response is related to the space charge polarization. The more specifically one can conclude that the number of defects are reduced due to the ions doping, consequently, degree of space charge polarization become reduced.

For a normal ferroelectric material, which undergoes a displacive phase transition, the dielectric constant  $\epsilon$  (*T*) obeys the well known Curie-Weiss law [22]

$$\epsilon = C / (T - T_0), \quad T > T_C, \tag{1}$$

$$\epsilon = C' / (T - T_1), \quad T < T_C, \tag{2}$$

where *C* and *C'* are the Curie constants and *T<sub>0</sub>* and *T<sub>1</sub>* are the extrapolated temperatures above and below *T<sub>C</sub>*, respectively and its follow the following relations near *T<sub>C</sub>*;

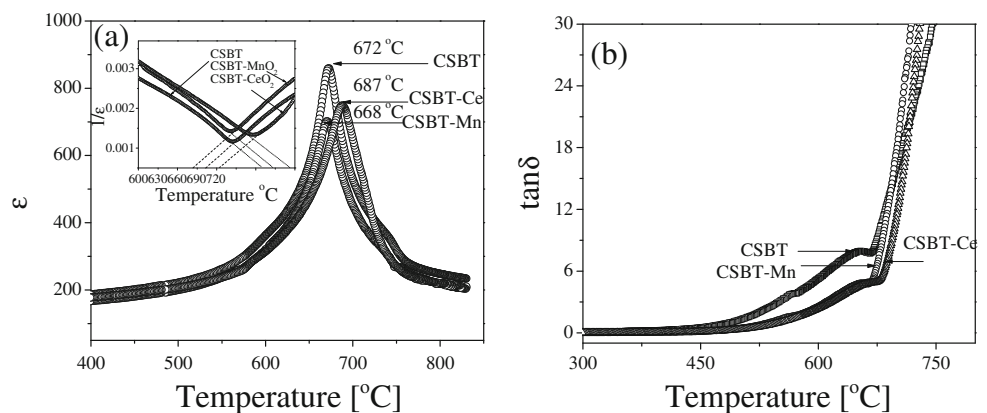
$$2^{\text{nd}} \text{ order} : T_0 = T_C = T_1 \text{ and } C' = C \quad \text{above } T_C, \tag{3}$$

$$1^{\text{st}} \text{ order} : T_0 < T_C < T_1 \text{ and } C' = 8 \text{ just below } T_C, \tag{4}$$

Therefore, the order of ferroelectric to paraelectric phase transition can be determined from the temperature dependent inverse plot of dielectric constant (1/ε). The reciprocal of dielectric constant vs temperature plot is shown in inset of Fig. 3(a). The obtained extrapolated temperature *T<sub>0</sub>* < *T<sub>C</sub>* and *T<sub>1</sub>* > *T<sub>C</sub>* satisfy the condition of a first order phase transition, while the Curie constant does not satisfy properly. However, a thermal hysteresis is clearly observed for all compositions (not shown) that supports the first order nature of a phase transition.

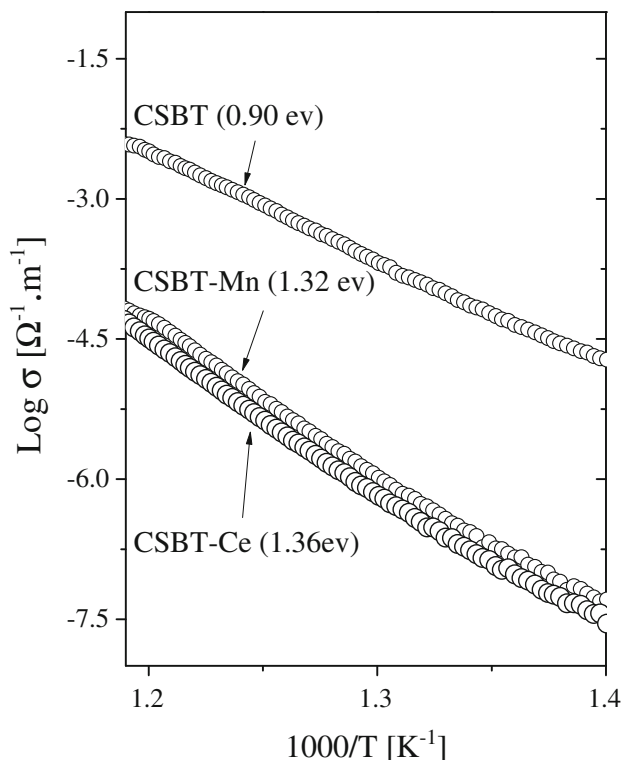
Figure 3(b) also shows the temperature dependence of dielectric loss (tanδ). At room temperature, it is very low for

**Fig. 3** (a) Temperature dependence of dielectric constants (inset: inverse plot of dielectric constant) and (b) Temperature dependence of dielectric loss of CSBT, CSBT-Mn, and CSBT-Ce ceramics



all compositions and remains constant up to 450°C and then increases drastically. This could be caused by a higher concentration of conduction carrier (positive and negative vacancies) especially at the higher temperature [20]. As, the samples were sintered at high temperature, therefore, the oxygen vacancy ( $V_O^{\bullet\bullet}$ ) is a common defect in the studied ceramics and the influences of  $V_O^{\bullet\bullet}$  become prominent at high temperature region (300–700°C) [20]. Due to the A-site replacement of  $Bi^{3+}$  and/or  $Ca^{2+}$  ion by  $Ce^{4+}$  ion may produce bismuth/or calcium vacancy,  $Ce'_{Bi}$ /or  $Ce''_{Ca}$ . These cation vacancies combined with  $V_O^{\bullet\bullet}$  produce  $[Ce'_{Bi}V_O^{\bullet\bullet}]$ /or  $[Ce''_{Ca}V_O^{\bullet\bullet}]$  types of defect dipole. In contrast, due to the B-site replacement of  $Mn^{3+}$  produce titanium vacancy  $Mn'_{Ti}$  that also combined with  $V_O^{\bullet\bullet}$  produce  $[Mn'_{Ti}V_O^{\bullet\bullet}]$  types of defect dipole. As a result, the  $\tan\delta$  decreases significantly due to the doping comprising with pure CSBT. The detail of defect chemistry can be found elsewhere [17, 23, 24].

The AC conductivity can be defined as  $\sigma = \omega \epsilon_0 \epsilon \tan\delta$ , where  $\omega$ ,  $\epsilon_0$ ,  $\epsilon$ , and  $\tan\delta$  are the angular frequency, permittivity of free space, relative permittivity, and loss tangent, respectively. Figure 4 shows the Arrhenius plot of  $\sigma$  within the temperature range 440–640°C and the calculated activation energy. It can be seen that the conductivity decreases considerably owing to the element doping especially at the high temperature region. At the low temperature region, the conductivity is presumably predominated by the extrinsic

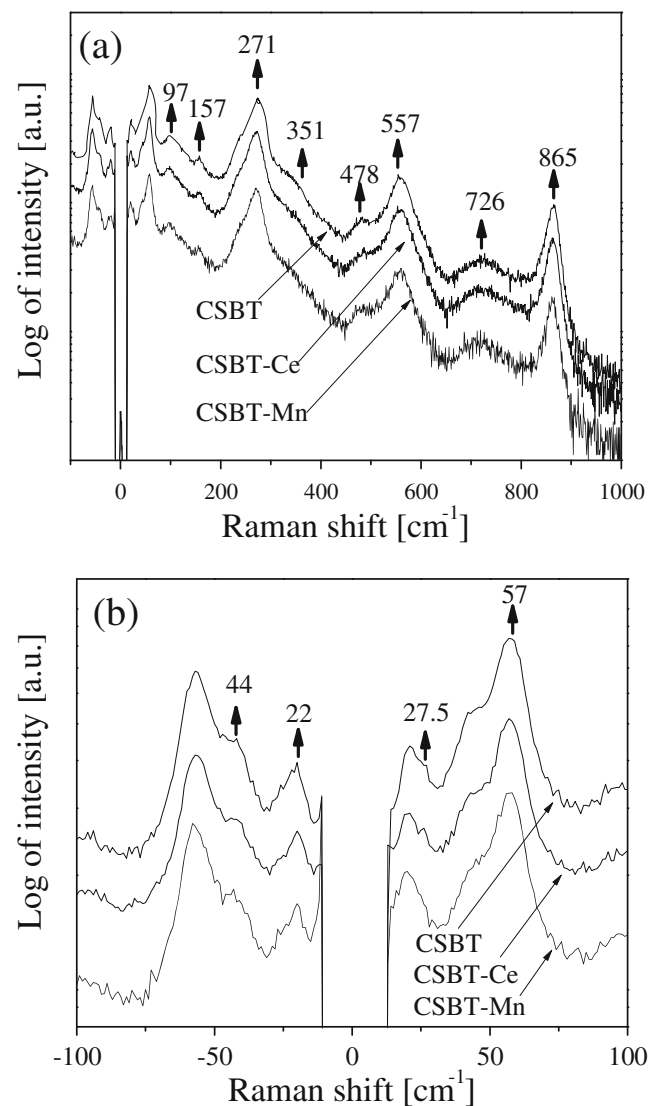


**Fig. 4** AC conductivity of CSBT, CSBT-Mn, and CSBT-Ce ceramics, as a function of temperature

defects, while at the high temperature region  $\sim 300\text{--}700^\circ\text{C}$  conduction is predominated by the intrinsic defects [20]. It is known that in a single phase materials with homogeneous microstructure the conductivity depends on both the mobility and concentration of the charge carries and the conductivity can be presented by the following empirical equations [10, 17]:

$$\sigma = nq\mu = \sigma_0 \exp(-E_a/k_B T) \quad (5)$$

where  $\sigma_0$  is a pre-exponential factors and a characteristic of materials,  $n$ ,  $q$ ,  $\mu$ ,  $E_a$ ,  $k_B$  and  $T$  is the concentration of charge carrier, number of charge per carrier, ionic mobility, activation energy for conduction, Boltzmann's constant, and absolute temperature, respectively. The improvement of conductivity can be explained by considering the bond



**Fig. 5** Room temperature Raman spectra of CSBT, CSBT-Mn, and CSBT-Ce ceramics in (a) the full range spectrum, and (b) the low frequency region



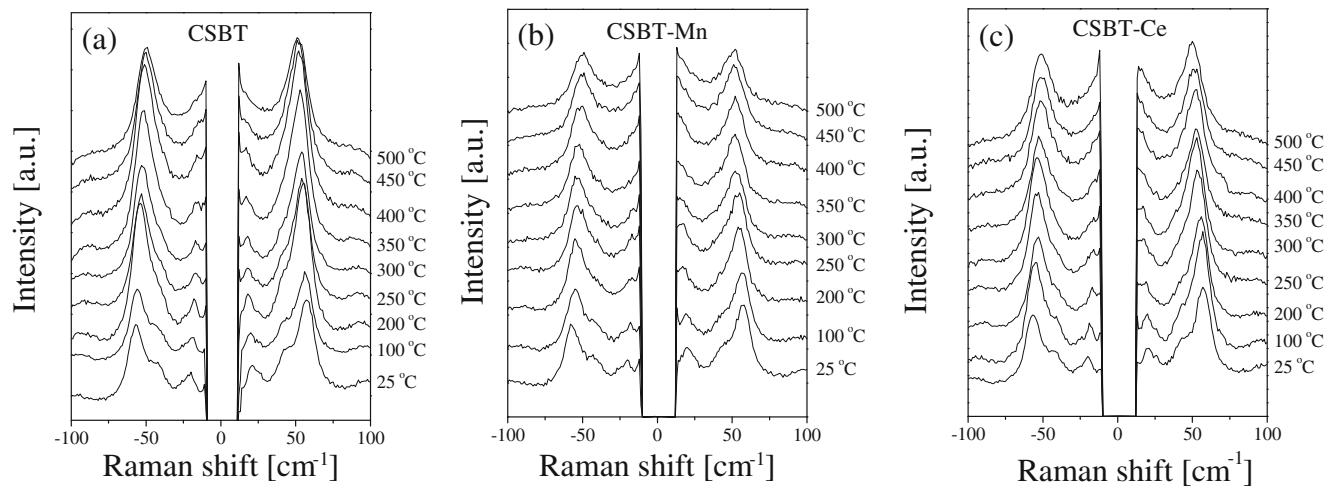


Fig. 6 Temperature dependence of Raman spectra of (a) CSBT, (b) CSBT-Mn, and (c) CSBT-Ce ceramics, in the low frequency region

energy. The bond energy of Mn-O in  $Mn_3O_4$  is 1386 kJ/mol, which is higher than the Ti-O (667kJ/mol) [15, 25]. On the other hand, the bond energy of Ca-O and Sr-O and Ce-O are  $383.3 \pm 5$ ,  $426.3 \pm 7$ , and  $790 \text{ kJ/mol}$ , respectively [25]. The substitution of  $Ce^{4+}$ ,  $Mn^{3+}$  and  $Mn^{3+}$  ions in the A and B-sites cations enhanced the stability of the perovskite lattice due to the increase of bond strength. The higher bond energy will effectively suppress the intrinsic defect formation. As a result, at elevated temperature, the electrical conductivity reduced significantly. The  $E_a$  of the CSBT, CSBT-Mn and CSBT-Ce are 0.90, 1.32 and 1.36 eV, respectively, calculated by using Eq. 3. This incrimination of activation energy is coherently related with the bond energy.

### 3.3 Raman scattering

Figure 5 shows the Raman spectra of the studied ceramics observed at room temperature. The Raman spectra exhibit intense phonon modes at 22, 57, 97, 157, 271, 478, 557, 726, and  $865 \text{ cm}^{-1}$  as well as some weak peaks. The phonon modes can be classified into two groups i.e. the internal modes of  $TiO_6$  octahedron located  $>200 \text{ cm}^{-1}$  and the lattice modes involved in the motion of the cations located  $<200 \text{ cm}^{-1}$ . The detailed of the mode identification was reported in literature [10, 26, 27]. The line shapes of spectra are almost invariant at room temperature, while the scattering intensity decreases drastically due to the  $CeO_2$  and  $MnO_2$  doping. It is well known that spectral intensity is related to the imaginary part of the dynamic susceptibility as well as the transmission property of the sample surface. The color of the studied sample become darkens due to the  $CeO_2$  and  $MnO_2$  doping [28]. Therefore, the observed reduction of scattering intensity may be caused by the sample color.

The low frequency Raman spectra at room temperature are shown in Fig. 5(b). Two sharp peaks are observed at 22

and  $57 \text{ cm}^{-1}$  as well as two shoulders appeared at 27.5 and  $44 \text{ cm}^{-1}$ . In BLSFs with  $m=3$  and 4, three soft modes are predicted: the relative  $a$ -axis displacement of Bi ions in the ferroelectric phase in the pseudo-perovskite layer with respect to the chain of a  $TiO_6$  octahedron at  $22 \text{ cm}^{-1}$ ; the rotational mode of the  $TiO_6$  octahedron along the  $a$ -axis at

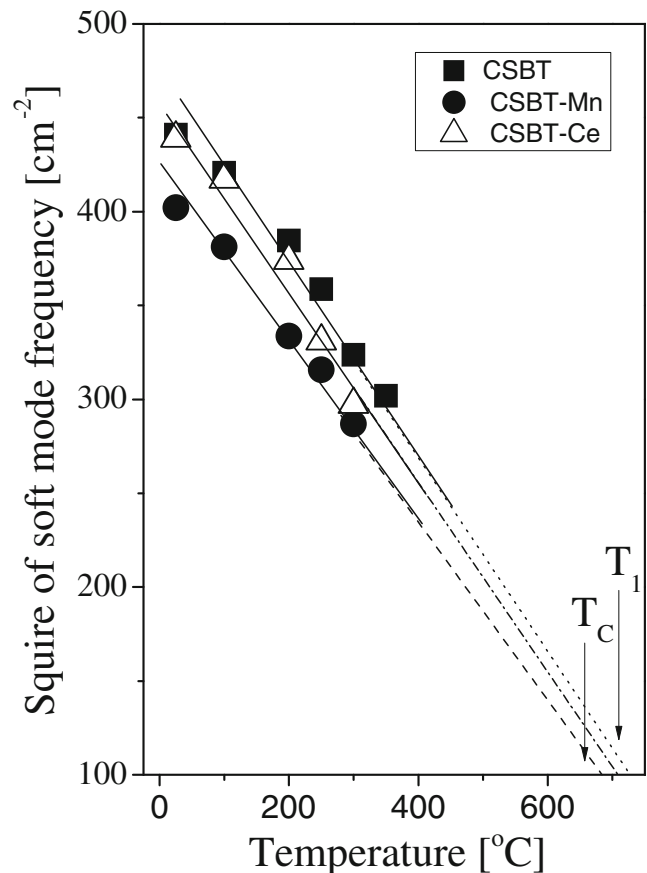


Fig. 7 The square of soft mode peak frequency of CSBT, CSBT-Mn, and CSBT-Ce ceramics, as a function of temperature

27.5  $\text{cm}^{-1}$ ; and another rotational mode of the  $\text{TiO}_6$  octahedron along the  $c$ -axis at 44  $\text{cm}^{-1}$  [9, 26, 27, 29]. The mode frequency at 22 and 44  $\text{cm}^{-1}$  slightly decreases, while the frequency of the rigid layer mode at 57  $\text{cm}^{-1}$  unchanged in CBT-Ce and CSBT-Mn. This fact indicates the occupation of A-site in the pseudo-perovskite layer by  $\text{Ce}^{4+}$  and  $\text{Mn}^{2+}$  ions.

To get new insights into the dynamics of the phase transition, the temperature dependence of soft optical phonon was investigated as shown in Fig. 6. With the increase of temperature the phonon modes at 27.5 and 44  $\text{cm}^{-1}$  become weak and broad, and finally disappear above 350° C. The rigid layer mode at 57  $\text{cm}^{-1}$  originated from the vibration of rigid  $\text{Bi}_2\text{O}_2$  layer also shifts toward the lower frequency, but still observed clearly up to 600°C. With the increase of temperature, the mode frequency at 22  $\text{cm}^{-1}$  shows a significant softening and finally overdamped around 500°C. Therefore, this mode can be a soft phonon mode, which is responsible to the structural phase transition. Figure 7 shows the temperature dependence of square of the soft mode peak frequency ( $\omega_s^2$ ), and it monotonically decreases towards the  $T_1$ , the extrapolated temperature at which  $\omega_s^2$  goes to zero. The fact  $T_1 > T_C$  is a common feature of a first order phase transition [10, 25]. While the damping of soft mode randomly increase with the increase of temperature that can be explained by considering the local strain in the pseudo-perovskite unit. The observed ratio approximately  $C : C' = 1 : 1$  and the difference between  $T_1$  and  $T_C$ , is rather small for all compositions. As there are some differences of ionic radii among the host (Ca, Sr, and Bi) and doping (Ce and Mn) ions that may induce some internal strain in the pseudo-perovskite unit. Such a local strain may couple with the soft optic mode. This coupling could be responsible for this dielectric anomalous behavior of  $C : C'$  ratios and the increase of damping of soft mode.

#### 4 Conclusions

The  $\text{CeO}_2$  and  $\text{MnO}_2$  doping effect on the dynamical physical properties of CSBT ceramics were investigated by using XRD, SEM, temperature dependent dielectric and Raman scattering measurements. The numerical values of dielectric constant were found as  $850 \pm 10$  (CSBT),  $740 \pm 10$  (CSBT-Ce), and  $690 \pm 10$  (CSBT-Mn) and the  $T_C$  of CSBT-Ce was enhanced from 672 (CSBT) to 687°C due to the crystal lattice distortion. The dielectric losses were reduced from 8 to 5 and the AC conductivity was decreased 2 times with in the temperature region  $\sim 500 \sim 700^\circ\text{C}$ , due to the reduction of conducting carriers through defect dipole formation. The

thermal hysteresis of a dielectric susceptibility and the fact that square of soft mode frequency  $\omega_s^2$  was approximately proportional to  $T_1 - T$  ( $T_C < T_1$ ) indicated the first order nature of a ferroelectric phase transition. The  $C : C'$  ratio was 1:1 and the scattered nature of damping constant of the soft optic mode demonstrated a coupling of soft mode with the local strain induced by doping. This coupling may enhance the piezoelectric performance of doped-CSBT.

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